

## Precision $\gamma$ -ray branching-ratio measurements for long-lived fission products of importance to stockpile stewardship

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We have measured the  $^{95}\text{Zr}$   $\beta$ -decay branching ratios to high ( $<1\%$ ) precision. This serves as a proof-of-principle demonstration that the method we have developed can be used to measure the  $\gamma$  rays and  $\beta$  branching ratios of long-lived fission products. As previously reported [1-2], we collected a high-purity sample of  $^{95}\text{Zr}$  (and its decay daughter  $^{95}\text{Nb}$ ) on a thin ( $40 \mu\text{g}/\text{cm}^2$ ) carbon-foil backing by using a low-energy mass-separated beam of  $A=95$  ions from CARIBU at Argonne National Lab. The subsequent decay measurements were performed at Texas A&M with the HPGe detector for  $\gamma$ -ray measurements and the Livermore  $4\pi$  gas counter for  $\beta$  counting.

We performed a thorough analysis of the collected data to obtain  $\gamma$ -ray intensities and  $\beta$  branching ratios in the decay of  $^{95}\text{Zr}$  and  $^{95}\text{Nb}$ . The  $\gamma$ -ray intensity ( $I_\gamma$ ) per  $\beta$  decay for a particular transition was determined from the  $\beta$ - $\gamma$  coincidence detection rate ( $R_{\beta\gamma}$ ) relative to the  $\beta$  particle detection rate from the decay of the isotope of interest ( $R_\beta$ ), through the relation

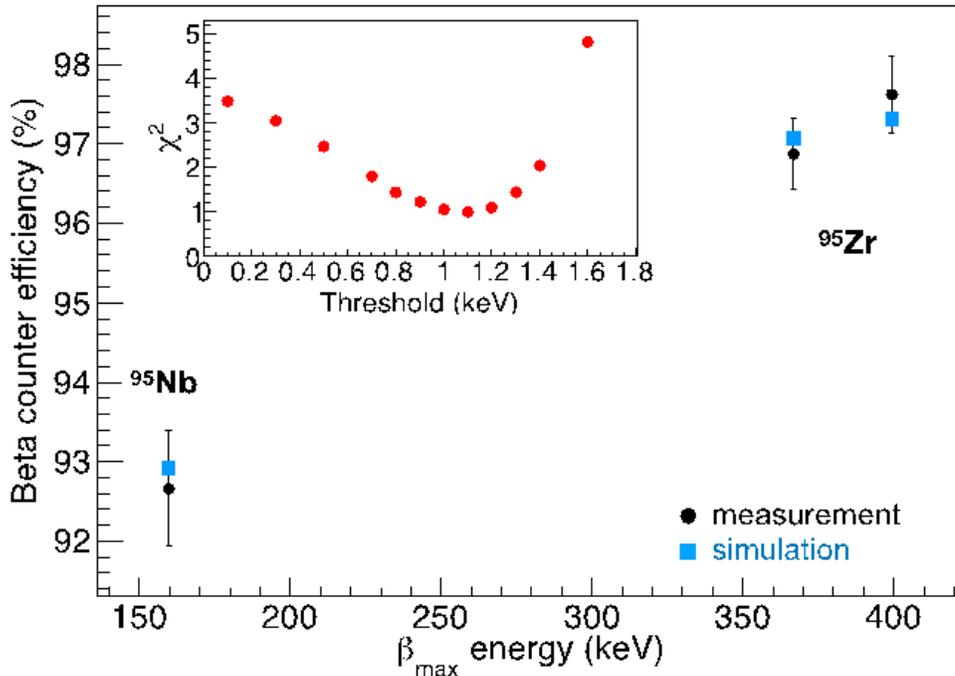
$$I_\gamma = \frac{R_{\beta\gamma}}{R_\beta} \frac{1}{\epsilon_\gamma} \frac{\epsilon_\beta}{\epsilon_{\beta\gamma}}.$$

Here  $\epsilon_\gamma$  is the photopeak efficiency of the HPGe detector for detecting the  $\gamma$  ray of interest. These efficiencies were obtained from the CYLTRAN simulation and are reported in Table I.  $\epsilon_{\beta\gamma}$  is the efficiency for detecting the  $\beta$  particles emitted in coincidence with that  $\gamma$  ray, and  $\epsilon_\beta$  is the efficiency for detecting the  $\beta$  particles from all decay branches of the isotope of interest in the  $4\pi$  gas counter. The  $\epsilon_\beta/\epsilon_{\beta\gamma}$  efficiency ratio of the  $4\pi$  gas proportional counter deviates from unity because the  $\beta$ -particle energy spectra in the ratio are not identical, and a different fraction of low-energy particles are lost to self-absorption in the carbon foil or to the electronic threshold of the counter. We determined the efficiency ratio using simulations of the detector response to the  $\beta$ -decay spectra under consideration.

**Table 1.** Detector efficiencies for the  $\gamma$  rays in the decay of  $^{95}\text{Zr}$  and  $^{95}\text{Nb}$ , and the  $\beta$  particle efficiency ratio for the  $4\pi$  gas counter.

Source	$E_{\gamma_i}$	$\epsilon_{\gamma_i}$ (%)	$E_{\beta_{max}}$	$\epsilon_\beta/\epsilon_{\beta\gamma}$
$^{95}\text{Zr}$	724.2 keV	0.2977(9)	399.4(18)	0.9987(1)
$^{95}\text{Zr}$	756.7 keV	0.2884(9)	366.9(18)	1.0011(1)
$^{95}\text{Nb}$	765.8 keV	0.2860(9)	159.8(5)	1.0000(1)

Before building the simulation model, we used the measured ratio of  $\beta$ - $\gamma$  coincidences over  $\gamma$  singles ( $R_{\beta\gamma}/R_\gamma$ ) to obtain the efficiency of the  $4\pi$  gas counter ( $\varepsilon_{\beta\gamma}$ ) for detecting the  $\beta$  particles emitted in coincidence with several detected  $\gamma$  rays. We then adjusted the  $\beta$ -detection threshold setting used in the simulation model to best reproduce those measured  $4\pi$  gas counter efficiencies. The comparison between the experiment and the simulation of the  $4\pi$  gas counter detector efficiency for the different  $\beta$ -decay transitions is presented in Fig. 1. The insert shows the  $\chi^2$  values obtained from the difference between the measured values and simulated values for a range of thresholds. These results indicate that the detector threshold was 1.1(3) keV. Table I shows the  $\varepsilon_\beta/\varepsilon_{\beta\gamma}$  efficiency ratios calculated with that threshold.



**FIG. 1.** Comparison of the measured gas counter efficiencies for the highest-intensity transitions in the decays of  $^{95}\text{Zr}$  and  $^{95}\text{Nb}$  to simulation results obtained with GEANT4 with a 1.1-keV threshold. The insert shows the  $\chi^2$  values obtained from the difference between the measured values and simulated values for a range of thresholds. These results indicated the detector threshold was 1.1(3) keV.

We calculated the  $\beta$ -decay branching ratios from the  $\gamma$ -ray intensities after including small contributions from conversion electron emission. The comparison between our results and the evaluated values [3] are presented in Table II. The complete uncertainty budget for  $\gamma$ -ray intensities from the decay of  $^{95}\text{Zr}$  and  $^{95}\text{Nb}$  is given in Table III. We are currently working on finalizing our results and uncertainties, and writing a manuscript that describes in detail our experimental approach, which will be submitted to the journal Nuclear Instruments and Methods in Physics Research A.

**Table II.** Preliminary results for the  $\gamma$ -ray intensities and  $\beta$  branching ratios for  $^{95}\text{Zr}$  and  $^{95}\text{Nb}$  obtained in this experiment in comparison with the evaluated values [3].

Isotope	$E_\gamma$	$I_{\gamma(\text{this work})}$	$I_\gamma$	$BR_{\beta(\text{this work})}$	$BR_\beta$
$^{95}\text{Zr}$	724.2 keV	0.4380(25)	0.4427(22)	0.4387(25)	0.4434(22)
$^{95}\text{Zr}$	756.7 keV	0.5441(28)	0.5438(22)	0.5449(28)	0.5446(22)
Ratio	724.2 keV/756.7 keV	0.805(6)	0.814(4)		
$^{95}\text{Nb}$	765.8 keV	0.9962(94)	0.9981(1)	0.9962(95)	0.9997(1)

**Table III.** The preliminary uncertainty budget for  $\gamma$ -ray intensities measured in this study.

Source	724.2 keV	756.7 keV	765.8 keV
$R_{\beta\gamma}$	0.0049	0.0041	0.0078
$R_\beta$	0.0008	0.0008	0.0044
$\epsilon_\gamma$	0.0030	0.0031	0.0031
$\epsilon_\beta/\epsilon_{\beta\gamma}$	0.0001	0.0001	0.0001
Total Uncertainty	0.0058	0.0052	0.0095

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